

**4/H-16 (iv) (Syllabus-2017)**

**2 0 2 3**

( May/June )

**ECONOMICS**

( Honours )

**( Mathematics for Economists )**

*Marks : 75*

*Time : 3 hours*

*The figures in the margin indicate full marks  
for the questions*

Answer **one** question from each Unit

**UNIT—I**

1. (a) Distinguish between equation and identity with suitable examples. 3
- (b) Given the universal set  $U$  as  $U = \{a, b, c, d, e, f\}$  and  $A = \{b, c, e\}$ ,  $B = \{a, c, d\}$ . Find—
- (i)  $(A^c - B^c)^c$
- (ii)  $(A \cup B^c)^c$
- (iii)  $(A \cap B^c)^c$
- (iv)  $(A \cap A^c)^c$  2×4=8

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- (c) In a group of 65 consumers, 50 of them consume apple while 20 of them consume both apple and orange. How many of them consume—

(i) orange;

(ii) orange only? 3+1=4

2. (a) What are simultaneous linear equations? How can these equations be used in solving economic problems? Give one example. 4

- (b) Determine the degree of homogeneity of the following functions : 3+3=6

(i)  $f(x, y) = x^3 - 5xy^2 + y^3$

(ii)  $f(L, K) = [3L^2 + 5K^2]^{1/2}$

- (c) The prices and quantities demanded for a particular commodity during two different periods are as follows :

	Prices	Quantities
Period-1	₹ 5	12 kg
Period-2	₹ 8	6 kg

Obtain the linear demand function.  
What would be the quantity demanded if the price was ₹ 9? 4+1=5

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UNIT—II

3. (a) Distinguish between diagonal matrix and identity matrix with suitable examples. Show that identity matrix is always idempotent. 3+2=5

(b) If

$$A = \begin{bmatrix} 3 & -2 \\ 4 & -1 \end{bmatrix} \text{ and } B = \begin{bmatrix} -6 & 5 \\ 3 & -4 \end{bmatrix}$$

then find the matrix  $D$  such that  $5A - 4B - 7D = 0$ . 5

- (c) What is determinant of a matrix? With suitable example, show that if two adjacent rows (or columns) of a given determinant are interchanged, then the given determinant gets multiplied by  $-1$ . 2+3=5

4. (a) If

$$A = \begin{bmatrix} 3 & -2 & -1 \\ 2 & 1 & 0 \\ -3 & 0 & 5 \end{bmatrix}$$

then prove that  $A^{-1} \cdot A = I$ . 6

- (b) Solve the following equations by Cramer's rule : 5

$$\frac{x}{3} - \frac{y}{6} = 1$$

$$\frac{x}{4} + \frac{y}{3} = 1$$

- (c) What is Leontief input-output model?  
State Hawkins-Simon conditions  
associated with this model.  $1+3=4$

## UNIT—III

5. (a) Under what conditions, a function  $f(x)$   
is said to be continuous at the point  
 $x=a$ ? Show that the following function  
is continuous at  $x=3$  :  $1+4=5$

$$f(x) = \begin{cases} x^2 - 5; & 0 < x < 3 \\ x + 1; & 3 < x < 6 \\ 2x - 2; & \text{otherwise} \end{cases}$$

- (b) Evaluate the following limits (any two) :  $2 \times 2 = 4$

(i)  $\lim_{x \rightarrow a} \frac{x^6 - a^6}{x^4 - a^4}$

(ii)  $\lim_{n \rightarrow \infty} \frac{3n^2 - 5n^{-1}}{4n^2 - 6n^{-2}}$

(iii)  $\lim_{h \rightarrow 0} \frac{(x+h)^3 - x^3}{5h}$

(iv)  $\lim_{x \rightarrow 2} \frac{x^3 - 8}{x^2 - 6x + 8}$

- (c) Find  $\frac{dy}{dx}$  of the following functions  
(any two) :  $3 \times 2 = 6$

(i)  $y = 3x^{-\frac{1}{2}} - 4x^{-\frac{3}{2}} + 10$

(ii)  $y = \log(x^2 - \sqrt{6-x} + 1)$

(iii)  $x + y + (x + y + 5)^3 = 0$

(iv)  $y = (x)^{\frac{1}{x}}$

6. (a) If

$$y = ax^2 + \frac{a}{x^2}$$

then prove that

$$x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} = 4y \quad 5$$

- (b) If  $u = x^3 - 4x^2y + y^3$ , then show that

$$\frac{\partial^2 u}{\partial x \partial y} = \frac{\partial^2 u}{\partial y \partial x} \quad 3$$

- (c) (i) If  $z = \sqrt{x+y}$ , then find  $dz$ .

(ii) If

$$z = \log \left( \frac{x-y}{x+y} \right)$$

then find  $dz$

where  $dz$  is the total differential  
of  $z$ .  $3+4=7$

## UNIT—IV

7. (a) Determine the maximum/minimum of the following function : 6

$$y = x^3 - 12x + 30$$

- (b) The demand function is given by  $x = \frac{30}{P+6}$ . Determine the price elasticity of demand if the price was ₹ 4. Also interpret the result. 6

- (c) If  $MR = ₹ 26$  and price elasticity of demand is 3, then find AR. 3

8. (a) The total cost function of the firm is  $C = 4x - x^2 + 2x^3$ . Show that when AC is minimum,  $AC = MC$ . 6

- (b) The demand function and total cost function are the following :

$$q = 100 - P$$

$$C = \frac{1}{3}q^3 - 7q^2 + 111q + 50$$

Determine the profit maximizing level of output ( $q$ ). Also write down the value of profit and the corresponding price ( $P$ ) at this level of output. 6+2+1=9

## UNIT—V

9. (a) What is integration? Why is there always a constant of integration? 1+2=3

- (b) Evaluate the following integral (any two) : 3×2=6

(i)  $\int x e^{-x} dx$

(ii)  $\int \frac{\log x}{x} dx$

(iii)  $\int (6x-5) \sqrt{3x^2-5x+1} dx$

(iv)  $\int x^2 e^{3x} dx$

- (c) The demand and supply functions are  $P_d = 26 - 5q$ ,  $P_s = 4q + 8$ . Find consumer's surplus. 6

10. (a) Explain briefly the concepts of definite and indefinite integral with examples. 2+2=4

- (b) Evaluate the following integral : 5

$$\int_{-a}^a (a^2 - ax + x^2) dx$$

- (c) The supply function is given by  $q = \sqrt{p-16}$ . Find the producer's surplus if the price was ₹ 20. 6

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